

PASSPORT THREE

ANSWERS

TOPICS	ANSWERS	TOPICS	ANSWERS																
1) Ratio	4 parts = $28l$ 1 part = $28 \div 4 = 7l$ Red Paint = $7 \times 3 = 21l$	13) Circles	Area Square = $15 \times 15 = 225\text{cm}^2$ Area Circle = $7.5^2 \times \pi = 56.25\pi$ Shaded = $225 - 56.25\pi = 48.3\text{cm}^2$																
2) Percentage Increase and Decrease	Casio = $0.85 \times 8.80 = £7.48$ Sharp = $0.74 \times 9.90 = £7.33$ The Sharp is cheaper by approx 15p	14) Semi Circles	Circumference = 3.6π Semi Arc Length = 1.8π Perimeter = $1.8\pi + 3.6 = 9.25\text{cm}$																
3) Best Buy	5 doughnuts = $£3.35 = 335p$ 1 doughnut = $335 \div 5 = 67p$ 2 doughnuts = $£1.38 = 138p$ 1 doughnut = $138 \div 2 = 69p$ The five doughnut deal is cheaper.	15) Angles in Polygons	Dec: Ext = 36° Int = 144° Pent: Ext = 72° Int = 108° $x = 144 - 108 = 36^\circ$																
4) HCF and LCM	a) $84 = 2 \times 2 \times 3 \times 7 = 2^2 \times 3 \times 7$ b) HCF = 12, LCM = 336	16) Angles on Parallel Lines	a) $84+32=116$ a = $180-116=64^\circ$ Alternate angles and angles on straight line. b) b - $180-64=116$ Vertically opposite and Interior angles.																
5) Estimation	$\frac{2 \times 300}{2^2} = \frac{600}{4} = 150$	17) Pythagoras	Base = $\sqrt{10^2 - 8^2} + \sqrt{12^2 - 8^2} = 14.9$ Area = $14.9 \times 8 \div 2 = 59.6\text{cm}^2$																
6) Standard From	a) $1.02 \times 10^{-3}, 2.1 \times 10^{-2}, 1.2 \times 10^3, 21000$ b) $768\ 000\ 000 = 7.68 \times 10^8$	18) Trigonometry	TOA Opp = $\tan(46) \times 8 = 8.28\text{cm}$																
7) Expand Double Brackets	a) $x^2 + 4x + 3x + 12 = x^2 + 7x + 12$ b) $x^2 - 5x + 7x - 35 = x^2 + 2x - 35$	19) Scatter Graphs	a) Positive c) 40-42cm																
8) Equations – 2 Steps	a) $7x = 84$ so $x = 12$ b) $\frac{x}{4} = -6$ so $x = -6 \times 4 = -24$	20) Pie Charts	Deg per item = $360 \div 120 = 3^\circ$ a) $26 \times 3 = 78^\circ$ b) $144 \div 3 = 48^\circ$ c) $46 \times 3 = 138^\circ$																
9) Equations Unknowns on Both Sides	a) $4x = 24$ so $x = 6$ b) $8x = 18$ so $x = \frac{18}{8} = 2\frac{1}{4}$	21) Frequency Polygon	Points (2,6), (6,2) and (12,5) plotted. Connected with straight lines. Axis clearly labelled.																
10) Form and Solve Equations	$4x + 40 = 360$ $4x = 320$ $x = 80^\circ$	22) Mean from a Table	a) $(50 + 1) \div 2 = 25.5\text{th}$ Median size 6 b) Mean = $328 \div 50 = 6.56$																
11) Functions	1) output = $12 - 5 = 7$ 2) Input = $(-1 + 5) \div 3 = \frac{4}{3} = 1\frac{1}{3}$	23) Mean from a Group Table	a) $(30 + 1) \div 2 = 15.5\text{th}$ Median class $10 < l \leq 15$ b) Mean = $390 \div 30 = 13$																
12) Quadratic Graphs	<table border="1"> <tr> <td>x</td><td>-3</td><td>-2</td><td>-1</td><td>0</td><td>1</td><td>2</td><td>3</td> </tr> <tr> <td>y</td><td>12</td><td>6</td><td>2</td><td>0</td><td>0</td><td>2</td><td>6</td> </tr> </table> <p>c) Solutions are $x_1 = (-2, 2)$, $x_2 = (2, 2)$</p>	x	-3	-2	-1	0	1	2	3	y	12	6	2	0	0	2	6	24) Venn Diagram	$P(O \cap S) = \frac{2}{10} = \frac{1}{5}$
x	-3	-2	-1	0	1	2	3												
y	12	6	2	0	0	2	6												

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NUMBER

TOPICS	ANSWERS	TOPICS	ANSWERS
Error interval	$345 \leq d < 355$	Reverse Percentage	$16.12 \div 0.55 = £29.31$
Percentage Decrease	$0.96 \times 2500 = £2400$	Percentage Change	$\frac{\text{change}}{\text{original}} \times 100$ $\frac{250,000 - 150000}{250,000} \times 100$ $= 16.7\%$
Index Notation	a) 1 b) $5 \times 5 \times 5 = 125$ c) $\sqrt{64} = 8$ d) $\frac{1}{3^7} = \frac{1}{2187}$	Standard Form	1) 2.54×10^5 2) 0.00105
Fractions and Percentages	15% in school $\frac{7}{20} = \frac{35}{100} = 35\%$ shopping $100 - (15 + 35) = 50\%$ cinema $0.5 \times 1400 = 700$ students went to the cinema	Subtracting and Multiplying Mixed Numbers	1) $\frac{19}{5} - \frac{9}{4} = \frac{76-45}{20} = \frac{31}{20} = 1\frac{11}{20}$ 2) $\frac{13}{3} \times \frac{23}{4} = \frac{299}{12} = 24\frac{11}{12}$

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Algebra

TOPICS	ANSWERS	TOPICS	ANSWERS
Factorising Expressions	<p>a) $4(x + 5)$ b) $3y(y + 4)$ c) $(x + 7)(x - 3)$</p>	Solving inequalities	$2x < 22$ $x < 11$
Solving Equations with Unknowns on Both Sides	$2x + 9 = -37$ $2x = -46$ $x = -23$	Simultaneous Equations	$8x = 48$ $x = 6$ $3x + 2y = 22$ $3(6) + 2y = 22$ $18 + 2y = 22$ $2y = 4$ $y = 2$
Change the Subject	<p>1) $3x = y - t$ $x = \frac{y - t}{3}$</p> <p>2) $\frac{x}{p} = z + pr$ $x = p(z + pr)$</p> <p>3) $tx + tr = p$ $tx = p - tr$ $x = \frac{p - tr}{t}$</p>	Midpoint of Coordinates	X coordinate $\frac{-4 + 10}{2} = \frac{6}{2} = 3$ Y Coordinate $\frac{6 + (-8)}{2} = \frac{-2}{2} = -1$ Midpoint $(3, -1)$
Gradient of a line	$\frac{\text{(Change in } y\text{)}}{\text{Change in } x} = \frac{\text{Rise}}{\text{Run}}$ $\text{Gradient} = \frac{4}{2} = 2$	Equation of a line parallel	$y = 2x + C$ E.g. $y = 2x$ $y = 2x - 1$ $y = 2x + 4$

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Shapes and Measures

TOPICS	ANSWERS	TOPICS	ANSWERS
Area of a Trapezium	$\frac{14 + 16}{2} \times 8 = \frac{30}{2} \times 8 \\ = 15 \times 8 = 120\text{cm}^2$	Bearings	$180 - 75 = 105^\circ$
Pythagoras' Theorem	$x = \sqrt{13^2 - 9^2} \\ x = 9.38\text{cm}$	Angles in Polygons	Exterior Angle $180 - 156 = 24^\circ$ Number of sides $\frac{360}{24} = 15 \text{ Sides}$
Volume of a Cylinder	$V = \pi \times 2.5^2 \times 9 \\ = 176.7\text{cm}^3$	Perimeter of a Sector	$\left(\frac{270}{360} \times \pi \times 18 \right) + 9 \\ + 9 \\ = 60.4 \text{ cm}$
Transformations – Enlargement from a point	Enlargement Scale Factor 2.5 Centre (0, 0)		

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Statistics

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Venn Diagram	<p>\mathcal{E}</p>																					
Mean from a table	<table border="1"> <thead> <tr> <th>Height (cm)</th> <th>Frequency</th> <th>MP</th> <th>Fx</th> </tr> </thead> <tbody> <tr> <td>$0 < h \leq 10$</td> <td>9</td> <td>5</td> <td>45</td> </tr> <tr> <td>$10 < h \leq 20$</td> <td>7</td> <td>15</td> <td>105</td> </tr> <tr> <td>$20 < h \leq 40$</td> <td>8</td> <td>30</td> <td>240</td> </tr> <tr> <td>$40 < h \leq 50$</td> <td>6</td> <td>45</td> <td>270</td> </tr> </tbody> </table> $\text{Mean} = \frac{660}{30} = 22\text{cm}$	Height (cm)	Frequency	MP	Fx	$0 < h \leq 10$	9	5	45	$10 < h \leq 20$	7	15	105	$20 < h \leq 40$	8	30	240	$40 < h \leq 50$	6	45	270	
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Sample Space	<table border="1"> <tr> <td></td> <td>1</td> <td>2</td> <td>3</td> <td>4</td> <td>5</td> <td>6</td> </tr> <tr> <td>Head</td> <td>1H</td> <td>2H</td> <td>3H</td> <td>4H</td> <td>5H</td> <td>6H</td> </tr> <tr> <td>Tail</td> <td>1T</td> <td>2T</td> <td>3T</td> <td>4T</td> <td>5T</td> <td>6T</td> </tr> </table> $P(H, \text{Even}) = \frac{3}{12} = \frac{1}{4}$		1	2	3	4	5	6	Head	1H	2H	3H	4H	5H	6H	Tail	1T	2T	3T	4T	5T	6T
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